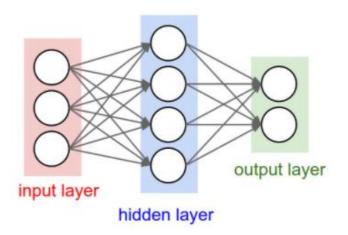


## Introduction to Deep Learning (I2DL)

Exercise 5: Neural Networks

## Today's Outline

- Universal Approximation Theorem
- Exercise 5
  - More numpy but structured



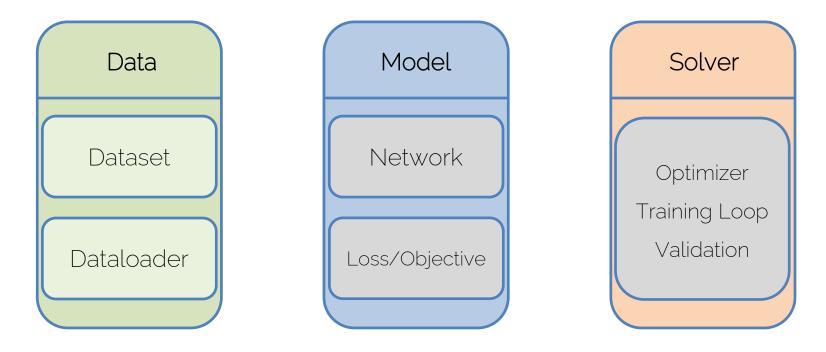
## Some background info

• You are currently in the numpy heavy part After exercise 5 there will be less numpy implementations



 Creating exercises is hard
 We will take your feedback to heart but we can't implement everything this semester with our current resources
 Feedback is still welcome and important!

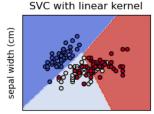
• The Pillars of Deep Learning



Back to the roots!

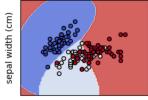
Common machine learning approaches:

- SVM
- Nearest Neighbors



sepal length (cm)

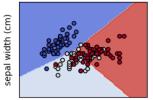
#### SVC with RBF kernel



sepal length (cm)

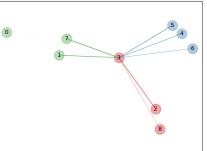


LinearSVC (linear kernel)



sepal length (cm)

Original points



Img src: scikit-learn.org, knowyourmeme "we don't do that here"

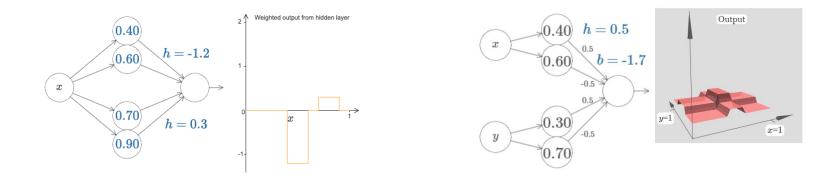


## Universal Approximation Theorem

## Universal Approximation Theorem

### Theorem (1989, colloquial)

For any continuous function f on a compact set K, there exists a one layer neural network, having only a single hidden layer + sigmoid, which uniformly approximates f to within an arbitrary  $\varepsilon > 0$  on K.



## Universal Approximation Theorem

Readable proof:

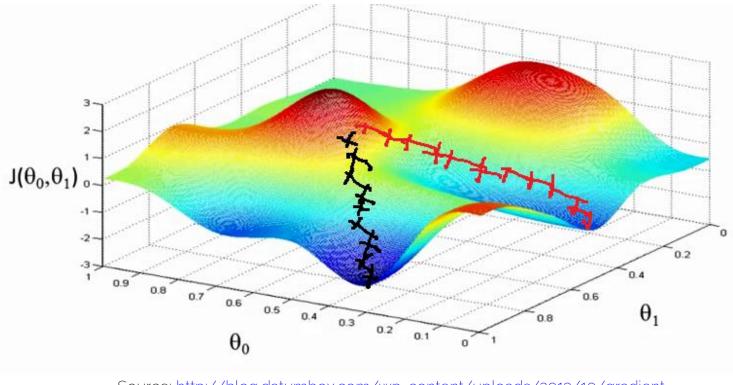
https://mcneela.github.io/machine\_learning/2017/03/21/ Universal-Approximation-Theorem.html

(Background: Functional Analysis, Math Major 3rd semester)

Visual proof:

http://neuralnetworksanddeeplearning.com/chap4.html

## A word of warning

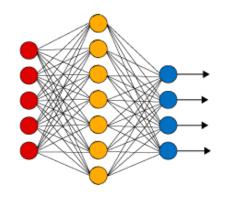


Source: <a href="http://blog.datumbox.com/wp-content/uploads/2013/10/gradient-descent.png">http://blog.datumbox.com/wp-content/uploads/2013/10/gradient-descent.png</a>

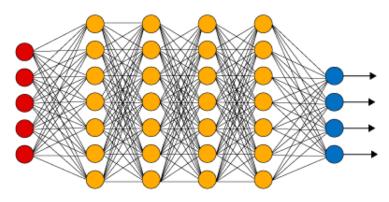
I2DL: Prof. Niessner

## How deep is your love

Shallow
 (1 hidden layer)



Deep
 (>1 hidden layer)



## **Obvious Questions**

Q: Do we even need deep networks?
 A: Yes. Multiple layers allow for more abstraction power given a fixed computational budget in comparison to a single layer -> better at generalization

- Q: So we just build 100 layer deep networks?
   A: Not trivially ;-)
  - Constraints: Memory, vanishing gradients, ...
  - deeper != working better



## Exercise 5

### Ex4:

- Small dataset And simple objective
- Simple classifier Single weight matrix



Ex5:

• CIFAR10

Actual competitive task

• Modularized Network Chain rule rules

• Gradient descent solver Whole forward pass in memory • Stochastic Descent

class Classifier(Network):	<pre>def forward(s)f(x):     """     Performs the forward pass of the model.</pre>
Classifier of the form y = sigmoid(X * W)	:para X: N x D array of training data. Each row is a D-dimensional point. :return Predicted labels for the data in X, shape N x 1
<pre>definit(self, num_features=2):     super(Classifier, self)init("classifier")</pre>	i-dimensional array of length N with classification scores.
<pre>self.num_features = num_features self.W = None</pre>	<pre># add a column of 1s to the data for the bias term batch_size, _ = X.shape X = np.concatenate((X, np.ones((batch_size, 1))), axis=1) # save the samples for the backward pass</pre>
<pre>def initialize_weights(self, weights=None) """ Initialize the weight matrix W</pre>	<pre># save the samples for the backward pass self.cache = X # outermariable y None</pre>
<pre>:param weights: optional weights for initialization """</pre>	######################################
<pre>if weights is not None: assert weights.shape == (self.num_features + 1, 1), \ "weights for initialization are not in the correct nape self.W = weights</pre>	<pre>Implement the forward pass and return the output of the model. Note # # that you need to implement the function self.sigmoid() for that # ###################################</pre>
<pre>else: self.W = 0.001 * np.random.randn(self.num_features + 1, 1)</pre>	y = self.sigmoid(y)
	######################################

## New: Modularization

## Chain Rule:

дf ∂d  $\partial d$ 



class Sigmoid: def \_\_init\_\_(self): pass def forward(self, x): """ :param x: Inputs, of any shape :return out: Output, of the same shape as x :return cache: Cache, for backward computation, of the same shape as x """

```
def backward(self, dout, cache):
```

.....

:return: dx: the gradient w.r.t. input X, of the same shape as X

## **Overview Exercise 5**

- One notebook
  - But a long one...

### deadline Wednesday <u>15:59</u>

Multiple smaller implementation objectives

#### Definition

$$CE(\hat{y},y) = rac{1}{N}\sum_{i=1}^{N}\sum_{k=1}^{C} \Big[-y_{ik}\log(\hat{y}_{ik})\Big]$$

where:

- +  $\,N$  is again the number of samples
- $C \ensuremath{\,\mathrm{is}}$  the number of classes
- $\hat{y}_{ik}$  is the probability that the model assigns for the k'th class when the i'th sample is the input.
- +  $y_{ik} = 1$  iff the true label of the ith sample is k and 0 otherwise. This is called a one-hot encoding.

#### Task: Check Formula

Check for yourself that when the number of classes C is 2, then binary cross-entropy is actually equivalent to cross-entropy.

### Outlook Ex6: CIFAR10 again run optimize( Parameters Hyperparameters Score n\_layers = 3 Weights n neurons = 512 85% optimization learning\_rate = 0.1 n\_layers = 3 Weights Ö n\_neurons = 1024 80% optimization learning rate = 0.01 n\_layers = 5 Weights n\_neurons = 256 92% optimization learning rate = 0.1



# See you next week